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Total No. of Pages : 02

Total No. of Questions : 18

B.Tech. (CE) (2018 Batch) (Sem.-3)

MATHEMATICS-III (TRANSFORM & DISCRETE MATHEMATICS)

Subject Code : BTAM-301-18

M.Code : 76373

Time : 3 Hrs.

Max. Marks : 60

INSTRUCTIONS TO CANDIDATES :

1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
2. SECTION-B contains FIVE questions carrying FIVE marks each and students have to attempt any FOUR questions.
3. SECTION-C contains THREE questions carrying TEN marks each and students have to attempt any TWO questions.

SECTION-A

Write briefly :

1. Prove that $\int \vec{r} \cdot d\vec{r} = 0$, where r has its usual meaning.
2. If $\vec{A} = 2xz\hat{i} + y\hat{j} - x^2\hat{k}$, $\vec{B} = x^2yz\hat{i} - 2xz^3\hat{j} - xz^2\hat{k}$ then find $\frac{\partial^2}{\partial x \partial y} (\vec{A} \times \vec{B})$ at $(1, 1, 1)$.
3. Show that $\text{curl curl } \vec{v} = \text{grad div } \vec{v} - \nabla^2 \vec{v}$ where \vec{v} is any vector.
4. If \vec{f} is solenoid vector then show that $\text{curl curl curl curl } \vec{f} = \nabla^4 f$.
5. Define Gradient and state its physical significance.
6. State and prove Second shifting property of Laplace transform.
7. Evaluate $L(\cos^2 \alpha t \sin \beta t)$.
8. Find finite Fourier sine transform of $f(t) = 1$.
9. Define Euler formulae.
10. State and prove change of scale property of laplace transform.

SECTION-B

11. Find directional derivative of $\phi = 3y^2 + yz^3$ at a point $(2, -1, 1)$ in the direction normal to the surface $x \log z - y^2 + 4 = 0$ at a point $(-1, 2, 1)$.
12. $\vec{f} = (2x^2 + y^2)\hat{i} + (3y - 4x)\hat{j}$, evaluate $\int_C \vec{f} \cdot d\vec{r}$ around the triangle ABC whose vertices are A $(0, 0)$, B $(2, 0)$ and C $(2, 1)$.
13. Using Laplace evaluate $\int_0^\infty t^3 e^{-t} \sin t \, dt$.
14. Find inverse laplace of $\frac{s^2}{(s^2 + \alpha^2)^2}$.
15. Use convolution theorem to find $F^{-1}\left(\frac{1}{12 - s^2 + 7is}\right)$.

SECTION-C

16. Verify Green's theorem in the XY-plane for $\oint_C (xy^2 - 2xy) \, dx = (x^2y + 3) \, dy$ around boundary C of the region enclosed $y^2 = 8x$ and $x = 2$.
17. The string is stretched between the points $(0, 0)$ and $(l, 0)$. If it is displaced along the curve $y = K \sin\left(\frac{\pi x}{l}\right)$ and released from rest in that position at time $t = 0$. Find the displacement $y(x, t)$ at any time $t > 0$ and at any point, $x, 0 < x < l$.
18. If $f(x) = \begin{cases} x, & \text{when } 0 < x < \frac{\pi}{2} \\ \pi - 2, & \text{when } \frac{\pi}{2} < x < \pi \end{cases}$ show that $f(x) = \frac{4}{\pi} \left[\sin x - \frac{\sin 3x}{3^2} + \frac{\sin 5x}{5^2} + \dots \right]$

NOTE : Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.